

Today's lecture:

- Bayesian networks

Bayes Theorem:

$$P(h|e) = P(e|h) \times P(h)/P(e)$$

Or:

$$P(h|e) = P(h \wedge e)/P(e)$$

Bayesian Exercise:

2 tests are given, 25% passed both tests, 42% passed the first. What is the probability that a student who passed the first test also passed the second?

$$P(\text{passed both}) = 0.25$$

$$P(\text{passed first}) = 0.42$$

$$P(\text{passed both}|\text{passed first})$$

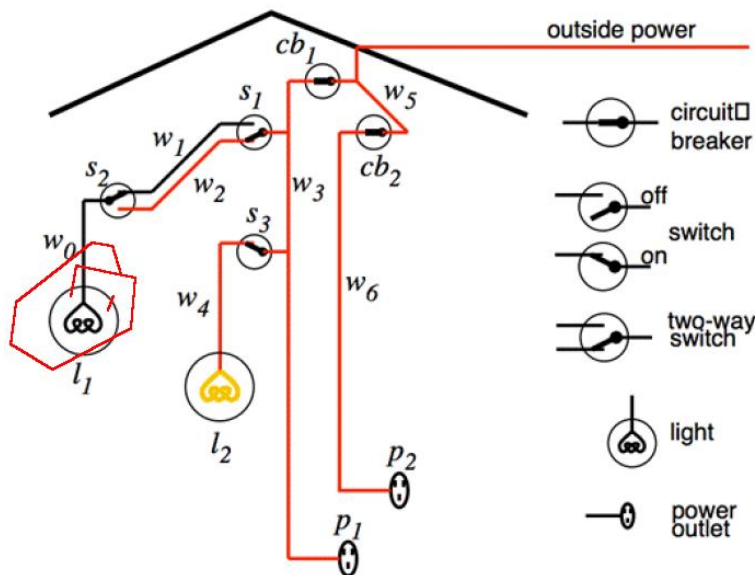
$$= P(\text{passed first}|\text{passed both}) \times P(\text{passed both})/P(\text{passed first}) =$$

$$1.0 \times 0.25/0.42 = 0.595$$

Conditional Independence:

- Random var X is **independent** of Y given Z if Y 's value does not affect one's belief in X 's value given the value of Z :
- $P(X = x|Y = y_1, Z = z) = P(X = x|Y = y_2, Z = z) = P(X = x|Z = z)$

Example: electrical circuit:



Example of conditional independence: in the slides

Belief Networks:

- Totally order the variables of interest: X_1, \dots, X_n
- The parents of X_i denoted $parents(X_i)$ are its predecessors that render X_i independent of other predecessors:

$$parents(X_i) \subseteq \{X_1, \dots, X_{i-1}\} \text{ and } P(X_i | parents(X_i)) = P(X_i | X_1, \dots, X_{i-1})$$

- So $P(X_1, \dots, X_n) = \prod_{i=1}^n P(X_i | parents(X_i))$
 - A **belief network** is a DAG where rand vars are nodes and edges are from parents to children
- ... (wimba got stuck)

Pruning irrelevant variables:

Suppose we want to compute $P(X | e_1, \dots, e_k)$

- Prune variables with no observed or queried descendants
- ...